

**I B. Tech I Semester Supplementary Examinations, May/June - 2019**  
**MATHEMATICS-II (NM&CV)**  
 (Com to ECE, EIE, ECom E)

Time: 3 hours

Max. Marks: 70

- Note: 1. Question paper consists of two parts (**Part-A** and **Part-B**)  
 2. Answering the question in **Part-A** is Compulsory  
 3. Answer any **FOUR** Questions from **Part-B**
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**PART -A**

1. a) Show that  $f(z) = |z|^2$  is not analytic at any point. (2M)
- b) Evaluate  $\int_0^{1+i} (x^2 + iy) dz$  along the paths (i)  $y = x$  (2M)
- c) Classify the Singularity of  $f(z) = \operatorname{Cosec} z$  at  $z = 0$  (2M)
- d) Find the Residue of  $f(z) = \frac{z}{(z+1)(z-2)}$  at  $z = -1$  (2M)
- e) Write the merits of modified Euler's method. (2M)
- f) Write relation between  $E$  and  $\delta$ . (2M)
- g) What is quadratic convergence? (2M)

**PART -B**

2. a) Find analytic function whose Real part  $u(x, y) = x^3 - 3xy^2 + 3x^2 - 3y^2 + 2x + 1$  (7M)
- b) Show that a analytic function  $f(z) = u + iv$  form an Orthogonal system. (7M)
3. a) find the Laurent's series of  $f(z) = \frac{z^2-1}{(z+2)(z+3)}$  for (7M)
  - (i)  $|z| > 3$  (ii)  $2 < |z| < 3$
- b) Evaluate  $\int_C \frac{e^{2z}}{(z-1)(z-2)} dz$  where  $C: |z| = 3$  using Cauchy's integral formula. (7M)
4. a) Evaluate  $\oint_C \frac{1+z}{z(2-z)} dz$  Where  $C: |z| = 1$  using residue theorem. (7M)
- b) Evaluate  $\int_0^\infty \frac{\sin mx}{x(x^2+a^2)} dx$  using residue theorem. (7M)
5. a) By Taylor's method find  $y(0.4)$  given that  $\frac{dy}{dx} = 3x + y^2, y(0) = 1$  (7M)
- b) Apply RK method of fourth order to find  $y(1.2)$  given that  $y' = x^2 + y^2, y(1) = 1.5$  (7M)

6. a) Interpolate by means of Newton backward formula, the population of a town for the year 1985, given that. (7M)

year	1939	1949	1959	1969	1979	1989
population	12	15	20	27	39	52

- b) Evaluate  $y(7)$  from the following table. (7M)

X	1	3	5	6	8
Y	2	1.5	2.4	4	5.6

7. a) Find the Real root of  $x + \log_{10} x - 2 = 0$  using Newton Raphson method. (7M)
- b) Find the Real root of  $\tan x = x$  using False position method. (7M)

