

III B. Tech I Semester Supplementary Examinations, June/July-2022
INFORMATION THEORY & CODING
(Electronics and Communication Engineering)

Time: 3 hours

Max. Marks: 75

Answer any **FIVE** Questions **ONE** Question from **Each unit**
 All Questions Carry Equal Marks

UNIT-I

- 1 a) Define coding efficiency. Derive the relation between coding efficiency and entropy. [8M]
 b) A source emits independent sequence of symbols from an alphabet consisting of five symbols from an alphabet with probabilities $1/4$, $1/8$, $1/8$, $3/16$, $5/16$ respectively. Find the Shannon code using Shannon encoding algorithm and compute the efficiency. [7M]

(OR)

- 2 a) What is information? Show that amount of information is equal to $-\log p(x_j)$ [8M]
 b) A source produces six message with probabilities $1/4$, $1/4$, $1/8$, $1/8$, $1/8$, $1/8$. Obtain the information content of each message and the entropy. [7M]

UNIT-II

- 3 a) Derive the relation between mutual information and entropy. [8M]
 b) A Gaussian channel has bandwidth of 1MHz. [7M]
 (i) Calculate the channel capacity if the signal power to noise spectral density ratio is 10^5 Hz.
 (ii) Find the maximum information rate.

(OR)

- 4 a) Prove $I(X;Y) = I(Y;X)$. [8M]
 b) What is channel capacity and channel efficiency? Define redundancy. [7M]

UNIT-III

5. a) For a systematic (6, 3) linear block code, the parity matrix 'P' is given by $P =$ [8M]

$$\begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{bmatrix}$$

- (i) Construct table for code words.
 (ii) If the received bit pattern $R = [1 \ 0 \ 1 \ 1 \ 0 \ 0]$, determine the syndrome, correctable error pattern and corrected code vector for a single bit error.



- b) Justify [7M]
 (i) For a 2 bit error detection $d_{\min} = 2$
 (ii) For a single bit error correction $d_{\min} = 3$
(OR)
6. a) Explain the following terms with necessary equations [8M]
 (i) Minimum distance
 (ii) Syndrome
 (iii) Generator matrix
 (iv) Parity check matrix
 b) Compare coded systems and un-coded system. [7M]
- UNIT-IV**
7. a) Design encoder for the (7, 4) binary cyclic code generated by $g(x) = 1 + x + x^3$ and verify the operation using the message vector {1 0 0 1}. [8M]
 b) (i) Differentiate systematic and non-systematic cyclic codes. [7M]
 (ii) Briefly explain cyclic hamming codes.
- (OR)**
8. a) Write the decoding procedure for BCH codes. [8M]
 b) For the (7, 4) single error correcting cyclic code using generator polynomial $g(x) = 1 + x + x^3$. Find all code vectors in systematic form. [7M]
- UNIT-V**
9. a) A convolution encoder has three flip flops, three modulo-2 adders and an output multiplexer. The generator sequence of the encoder are as follows: $g(1) = (1, 0, 1)$, $g(2) = (1, 1, 0)$, $g(3) = (1, 1, 0)$. Draw the block diagram of the Convolution encoder. Also find the convolution code for message sequence $m = \{1 1 0 1 0\}$. [8M]
 b) What are convolutional codes? How are they different from block codes? [7M]
- (OR)**
10. a) Give the Viterbi Algorithm's procedural steps with an example. [8M]
 b) If the input sequence is 1010, draw the code tree and specify the outputs at each state. [7M]

